

Tender Heart High School, Sector 33B, Chd.

Class 9th, Mathematics

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Date: 9.12.2024

REVISION TEST (Ch 17 & 18)

Ques.1: Find the area of a triangle whose sides are 34cm, 20cm and 42cm. Hence, find the length of the altitude corresponding to the shortest side.

Ques.2: Find the area of an equilateral triangle whose side is 8m. Give your answer correct to two decimal places.

Ques.3:- If the lengths of the sides of a triangle are in the ratio 3:4:5 and its perimeter is 48cm, find its area.

Ques.4:- Find the area of an isosceles triangle whose base is 6cm and perimeter is 15cm.

Ques.5:- If the area of a semi-circular region is 77cm^2 , find its perimeter.

Ques.6:- The wheel of a cart is making 5 revolutions per second. If the diameter of the wheel is 84cm, find its speed in km/h. Give your answer, correct to the nearest km.

Ques.7:- The circumference of a circle is 123.2cm. Calculate:-

- (i) the radius of the circle in cm.
- (ii) the area of the circle in cm^2 , correct to the nearest cm^2

Ques.8:- The sum of diameters of two circles is 14cm and the difference of their circumferences is 8cm. Find the circumference of the two circles.

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Solution of Revision Test-3

Sol.1:- Consider 34cm, 20cm and 42cm as the sides of triangle. Let $a = 34\text{cm}$, $b = 20\text{cm}$ and $c = 42\text{cm}$

$$s = \text{semi perimeter} = \frac{a+b+c}{2} = \frac{34+20+42}{2} \\ = \frac{96}{2} = 48\text{cm}$$

$$\begin{aligned} \text{Area of triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{48(48-34)(48-20)(48-42)} \\ &= \sqrt{8 \times 6 \times 14 \times 14 \times 2 \times 6} \\ &= 14 \times 6 \sqrt{8 \times 2} \\ &= 14 \times 6 \times 4 = 336\text{cm}^2 \end{aligned}$$

Here, the shortest side of the triangle is 20cm

$$\text{Area of triangle} = \frac{1}{2} \times \text{base} \times \text{height}$$

$$336 = \frac{1}{2} \times 20 \times h$$

$$\Rightarrow h = \frac{336 \times 2}{20} = 33.6\text{cm}$$

Sol.2:- side of equilateral triangle = 8m

$$\begin{aligned} \text{Area of equilateral triangle} &= \frac{\sqrt{3}}{4} (\text{side})^2 \\ &= \frac{\sqrt{3}}{4} \times 8 \times 8 \\ &= \sqrt{3} \times 16 = 16\sqrt{3} \end{aligned}$$

$$= 16 \times 1.732 = 27.71\text{m}^2$$

Class 9th, Mathematics

Sol 3:- Let the sides are $3x$, $4x$ and $5x$
 Given perimeter = 48cm

$$\text{Semi-perimeter} = \frac{3x + 4x + 5x}{2} = \frac{48}{2} = 24\text{cm}$$

$$\Rightarrow \frac{12x}{2} = \frac{48}{2} \Rightarrow x = 4\text{cm}$$

Here, $s = 24$, $a = 12$, $b = 16$, $c = 20\text{cm}$

$$\begin{aligned} \text{Area of triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{24(24-12)(24-16)(24-20)} \\ &= \sqrt{24 \times 12 \times 8 \times 4} \\ &= 12 \times 4 \times 2 = 96\text{cm}^2 \end{aligned}$$

Sol 4:- Base of triangle = 6cm , Perimeter = 16cm
 Let the other two equal sides are $x\text{cm}$ each
 Then, perimeter of triangle = $x + x + 6 = 16\text{cm}$
 $\Rightarrow 2x = 10\text{cm} \Rightarrow x = 5\text{cm}$ each.

So, the sides of triangle are 5cm , 5cm and 6cm

By using Heron's Formula,

$$\text{Area of triangle} = 12\text{cm}^2$$

Sol 5:- Area of a semicircular region = 77cm^2

Consider r as the radius of the region

$$\text{Area} = \frac{1}{2} \pi r^2 \Rightarrow \frac{1}{2} \times \frac{22}{7} \times r^2 = 77$$

$$\Rightarrow r^2 = \frac{77 \times 2 \times 7}{22} = 49 = 7^2$$

$$\Rightarrow r = 7\text{cm} \quad \text{Perimeter of the region} \\ = \pi r + 2r$$

Class 9th, Mathematics

$$= \frac{22}{7} \times 7 + 2 \times 7 = 22 + 14 = 36 \text{ cm}$$

Sol. 6:- Diameter of wheel = 84 cm

$$\text{Radius of wheel} = \frac{84}{2} = 42 \text{ cm}$$

$$\begin{aligned} \text{Here, Circumference of wheel} &= 2\pi r \\ &= 2 \times \frac{22}{7} \times 42 = 264 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{So, the distance covered in 5 revolutions} \\ &= 264 \times 5 = 1320 \text{ cm} \end{aligned}$$

$$\text{Time} = 1 \text{ second}$$

$$\begin{aligned} \text{Speed of wheel} &= \frac{1320 \times 60 \times 60}{1 \times 100 \times 1000} \\ &= 47.25 \text{ km/hr} \\ &= 48 \text{ km/hr.} \end{aligned}$$

Sol. 7:- Circumference of circle = 123.2 cm

$$\Rightarrow 2\pi r = 123.2 \Rightarrow 2 \times \frac{22}{7} \times r = 123.2 \text{ cm}$$

$$\Rightarrow r = \frac{123.2 \times 7}{2 \times 22} \Rightarrow 19.6 \text{ cm}$$

(ii) Here, Area of the circle = πr^2

$$\text{Substituting the values} = \frac{22}{7} \times 19.6 \times 19.6$$

$$= 1207.36$$

$$= 1207 \text{ cm}^2$$

Sol. 8:- Hint:- $2R + 2r = 14 \Rightarrow R + r = 7 \dots (i)$

$$2\pi R - 2\pi r = 8 \Rightarrow \pi(R - r) = 4 \dots (ii)$$

$$\text{So, } R = \frac{91}{22} \text{ and } r = \frac{63}{22} \Rightarrow 2\pi R = 18 \text{ cm}$$

$$\text{and } 2\pi r = 26 \text{ cm}$$