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Page - 1

TENDER HEART HIGH SCHOOL, SEC-33 B, CHD.

Subject: - PHYSICS ; TEACHER: - CHARANJEET KAUR

CLASS - X

NUMERICALS CHAPTER - 2(b)

WORK POWER AND ENERGY

① mass of Body A = mass of Body B = m

height of Body A ; $h_A = h$

" " B ; $h_B = 2h$

Ratio of their gravitational P.E is $\frac{mgh_A}{mgh_B} = \frac{mgh}{mg(2h)}$

$\Rightarrow \frac{1}{2}$ or 1:2

" " " " 1:2

② $m = 1\text{ kg}$, $h = 5\text{ m}$, $g = 10\text{ m/s}^2$

gravitational P.E = $mgh = 1 \times 5 \times 10 = 50\text{ J}$

Now K.E of the mass when it falls and hits the ground is 50 J ($\because$ When mass hits the ground its P.E is converted into K.E)

③ $m = 300\text{ kg}$, $g = 9.8\text{ N/kg}$, gravitational P.E = 29400 J

gravitational P.E = mgh

$29400 = 300 \times 9.8 \times h$

$10 = \frac{29400}{300 \times 9.8} = h$

$\boxed{h = 10\text{ m}}$

④ $m = 10\text{ kg}$, $h_1 = 20\text{ m}$, $h_2 = 8\text{ m}$, $g = 10\text{ m/s}^2$

(i) Loss in P.E = $mgh_1 - mgh_2 = mg(h_1 - h_2) = 10 \times 10 \times 12 = 1200\text{ J}$

(ii) Total Energy at any instant = ?

At height 20m ; P.E = $mgh = 10 \times 10 \times 20 = 2000\text{ J}$

" " ; K.E = 0 (Body is at rest)

So Total Energy = K.E + P.E = $2000\text{ J} + 0 = 2000\text{ J}$

⑥ $m = 50 \text{ kg}$, $h_1 = 3 \text{ m}$, $h_2 = 9 \text{ m}$

$$\begin{aligned} \text{Increase in Potential Energy} &= mg(h_2 - h_1) \\ &= 50 \times 10 (9 - 3) \\ &= 50 \times 10 \times 6 \text{ J} \\ &= 3000 \text{ J} \end{aligned}$$

⑧ $m = 50 \text{ kg}$, $h = 15 \text{ m}$, $g = 9.8 \text{ m/s}^2$

(i) work done by the man $= mgh = 50 \times 9.8 \times 15 = 7350 \text{ J}$

(ii) Increase in P.E. = ?

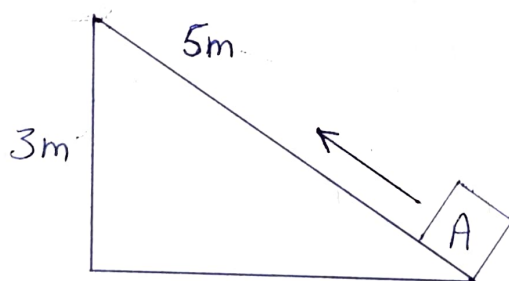
As the man climbs the ladder

So man's initial height is $= 0$ (before climbing)

" final " " $= 15 \text{ m}$ (After ")

$$\begin{aligned} \text{So, therefore Increase in P.E} &= mg(15 - 0) \\ &= 50 \times 9.8 \times 15 = 7350 \text{ J} \quad \underline{\text{Ans}} \end{aligned}$$

⑨



$$F = 100 \text{ N}, S = 5 \text{ m}$$

(i) work done by the force F ;
in moving the block A, 5 m
along the slope is

$$\begin{aligned} W &= FS \cos 0^\circ \quad (\text{Along the slope as } F \text{ \&S are same direction}) \\ W &= FS \\ W &= 100 \times 5 \end{aligned}$$

$$\boxed{W = 500 \text{ J}}$$

(ii) P.E. gained by the Block = ?

As block is moved through ^{the} vertically height of 3 m

$$\text{So P.E. gained} = mgh = 100 \times 3 = 300 \text{ J}$$

$$(\because F = mg = 100 \text{ N})$$

(iii) The difference in work done by the force and the increase in P.E. of the block is $= 200 \text{ J}$ ($\because 500 \text{ J} - 300 \text{ J} = 200 \text{ J}$)

$\therefore$ In moving this block through the slope, some energy is used in work done against the friction which is lost in the form of heat energy.

(11) $K.E = \frac{1}{2}mv^2 \Rightarrow K_1$

$K_2 = K.E \text{ for speed halved} = \frac{1}{2}m\left(\frac{v}{2}\right)^2 \quad \left[\because v' = \frac{1}{2}v\right]$

$$= \frac{1}{2}m \frac{v^2}{4}$$

$$= \frac{1 \cdot 1}{4 \cdot 2}mv^2$$

$$\boxed{K_2 \Rightarrow \frac{1}{4} \cdot K_1}$$

So new K.E becomes one fourth of K_1

(12)

mass of Body 1 = mass of Body 2 = m

velocity of Body 1 = v

" " " 2 = $2v$

$\because$ mass of the bodies are same $\therefore K.E \propto v^2$

$$\therefore K_1 = v^2 = v^2$$

$$K_2 = (2v)^2 = 4v^2$$

$$\text{or } \frac{K_1}{K_2} = \frac{v^2}{4v^2} = \frac{1}{4}$$

$$\text{or } \boxed{K_1 : K_2 = 1 : 4}$$

(13)

one Car running with speed = 15 km/hr

Another Car " " " = 45 kmh^{-1}

K.E is directly proportional to v^2 if mass is same then:

$$K_1 = v_1^2 = (15)^2$$

$$K_2 = v_2^2 = (45)^2$$

$$\text{or } \frac{K_1}{K_2} = \left(\frac{15}{45}\right)^2$$

$$\frac{K_1}{K_2} = \left(\frac{1}{3}\right)^2 = \frac{1}{9}$$

$$\text{or } \boxed{K_1 : K_2 = 1 : 9}$$

(17)

$$m = 10 \text{ kg}, v = 20 \text{ m/s}$$

$$m' = 2 \times 10 = 20 \text{ kg}$$

$$v' = \frac{1}{2} \times 20 = 10 \text{ m/s}$$

$$\text{Initial K.E} = \frac{1}{2} m v^2 = \frac{1}{2} \times 10 \times (20)^2 = 5 \times 400 = 2000 \text{ J}$$

$$\text{Final K.E} = \frac{1}{2} m' v'^2 = \frac{1}{2} \times 20 \times (10)^2 = \frac{1}{2} \times 20 \times 10 \times 10 = 1000 \text{ J}$$

(19)

$$m = 60 \text{ kg}, p = 3000 \text{ kg m}^{-1} \text{ s}$$

$$\text{Ci) } K.E = \frac{p^2}{2m} \quad \left[\because p^2 = 2mk \right]$$

$$K.E = \frac{3000 \times 3000}{2 \times 60} \quad \text{as } k \text{ is } K.E$$

$$K.E = 75000 = 75 \times 10^3 = 7.5 \times 10^4 \text{ J} \quad \text{or}$$

Cii) Speed of body (v) = ?

$$K.E = \frac{1}{2} m v^2$$

$$75000 = \frac{1}{2} \times 60 \times v^2$$

$$\frac{2 \times 75000}{60} = v^2$$

$$v^2 = 2500$$

$$v = \sqrt{2500} = 50 \text{ m/s} \quad \text{Ans}$$

(20)

$$m = 50 \text{ g} = \frac{50}{1000} \text{ kg} = 5 \times 10^{-3} \text{ kg}$$

$$p = 5 \text{ kg m s}^{-1}$$

Work done = K.E (to give momentum to body)

$$K = \frac{p^2}{2m}$$

$$K = \frac{5 \times 5}{2 \times 5 \times 10^{-3}} = \frac{25}{2 \times 5 \times 10^{-3}} = \frac{25}{10^{-2}} = 2.5 \times 10^3 = 2500 \text{ J} \quad \text{Ans}$$

$$\left(\because p^2 = 2mk \right)$$

$$\left(\frac{p^2}{2m} = k \right)$$

Q(21) (a) work done by the man carrying the box for 5 minutes;
= Zero ($\because$ he is stationary not covering any displacement)

(b) ^ghe runs carrying the box with a speed of 3 m/s to catch the bus:-

$$\begin{aligned}\text{So work done} &= \text{K.E of man} \\ &= \frac{1}{2}mv^2 \\ &= \frac{1}{2} \times 20 \text{ kg} \times (3)^2 = \frac{1}{2} \times 20 \times 3 \times 3 \\ &= 90 \text{ J}\end{aligned}$$

(c) If he raises the box by 0.5 m;

$$\begin{aligned}\text{P.E gained by him is } mgh &= 20 \times 10 \times 0.5 \\ &= 20 \times 10 \times 5\end{aligned}$$

($g = 10 \text{ ms}^{-2}$)

$$\boxed{\text{P.E} = 100 \text{ J}}$$

Q(22) bullet mass = 50 g = $\frac{50}{1000} = 5 \times 10^{-2} \text{ kg}$, $v = 500 \text{ m/s}$.

$$\begin{aligned}\text{(a) K.E of the bullet} &= \frac{1}{2} \times 5 \times 10^{-2} \times 500 \times 500 \\ &= \frac{5 \times 250 \times 500}{10^2} \\ \text{K.E} &= 6250 \text{ J}\end{aligned}$$

(b) Average retarding force offered by the target (F) = ?

as work done by the bullet = K.E of the bullet

$$\text{work done} = \text{Force} \times \text{displacement}$$

$$6250 = F \times 0.1 \text{ m}$$

$$\frac{6250}{0.1} = F$$

$$\boxed{F = 76250 \text{ N}}$$

[displacement = 10 cm]

[bullet entered 0.1 cm
displacement in target = $\frac{10}{100} = 0.1 \text{ m}$]

23

$$m = 0.5 \text{ kg}$$

$$v = 2 \text{ m/s}$$

P.E of the Spring during Compression = K.E of moving trolley.

$$\therefore K.E = \frac{1}{2} \times m \times v^2 = \frac{1}{2} \times 0.5 \times 2 \times 2$$

$$K.E = 1 \text{ J}$$

or P.E of spring = 1 J Ans

finish

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