

Class 10, Mathematics

Chapter

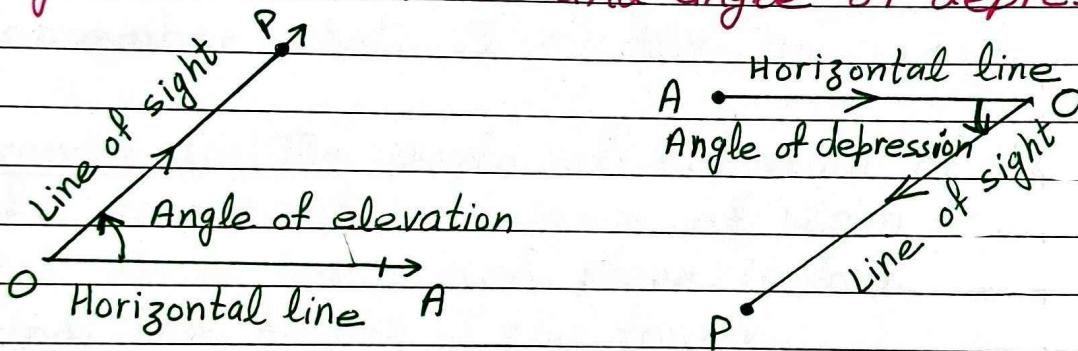
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Heights and Distances

Introduction:-

→ In this chapter, we will learn the practical use of trigonometry in our day-to-day life. We will see how trigonometry is used for finding the height and distances of various objects i.e. mountain (pillar or minar), breadth of a river, etc., which are otherwise very difficult to measure.

Angle of elevation and angle of depression

Line of sight:-

When the eye of a person at a point O looks at an object P, then the line OP is called the line of sight.

Angle of Elevation:-

Suppose a man from a point 'O', looks up at an object P, placed above the level of his eye. Then, $\angle POA$ is called the angle of elevation at P as seen from O.

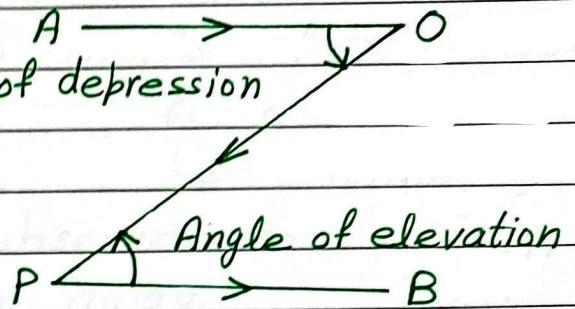
Angle of Depression:-

Suppose a man from a point 'O', looks down at an object P, placed below the level of his eye. Then, $\angle AOP$ is the angle of depression of P as seen from O.

→ Angle of depression
of P as seen from O

= Angle of elevation
of O as seen from P

$$\Rightarrow \angle AOP = \angle BPO$$



Note :- In problems on heights and distances,
usually, we find

required side = a certain t-ratio of a known
known side angle.

Remember that $\sqrt{2} = 1.414$ and $\sqrt{3} = 1.732$

15 Example 1:- The angle of elevation of the top
of a tower at a distance of 120m from its
foot on a horizontal plane is found to be 30° .
Find the height of the tower.

20 Solution:- Let AB be the tower and C
be the point of observation.

$$\therefore BC = 120\text{ m}$$

Since, angle of elevation is 30°

$$\therefore \angle ACB = 30^\circ$$

In $\triangle ABC$, $\frac{AB}{BC} = \frac{\text{Perp.}}{\text{Base}} = \tan \theta$ C - 120m - B

$$\Rightarrow \frac{AB}{120} = \tan 30^\circ$$

$$\Rightarrow AB = 120 \times \frac{1}{\sqrt{3}} = \frac{120}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \frac{120\sqrt{3}}{3} = 40\sqrt{3}$$

$$= 40 \times 1.732 = 69.28\text{ m}$$

Example 2:- An observer 1.5m tall is 28.5m away from a chimney. The angle of elevation of the top of the chimney from his eye is 45° . What is the height of the chimney?

Solution:- Let CD be an observer of height 1.5m which is 28.5m away from a chimney

AB of height h metres

$$CD = 1.5 \text{ m} \text{ and } DB = 28.5 \text{ m}$$

From C, draw CE \perp AB, then

CDBE is a rectangle.

$$AE = AB - BE = AB - CD = h - 1.5$$

$$\text{and } CE = DB = 28.5 \text{ m}$$

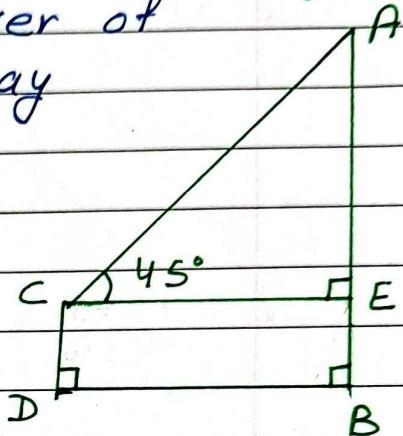
Given, angle of elevation $\angle ACE = 45^\circ$

From right angled $\triangle ACE$, we get

$$\tan 45^\circ = \frac{AE}{CE} \Rightarrow 1 = \frac{h - 1.5}{28.5}$$

$$\Rightarrow h - 1.5 = 28.5 \Rightarrow h = 30$$

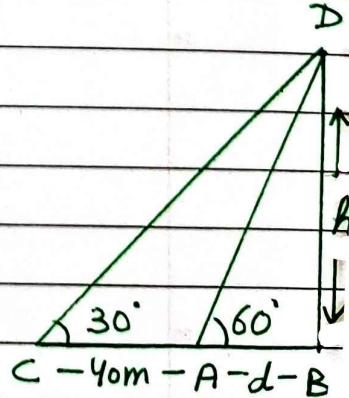
Hence, the height of the chimney = 30m



Example 3:- The shadow of a tower standing on a level ground is found to be 40m longer when the sun's altitude is 30° than when it is 60° . Find the height of the tower.

Solution:- Let the height of the tower BD be h metres and the length of its shadow be 'd' metres when the sun's altitude i.e. elevation is 60° .

When the sun's altitude is 30° , then the length of shadow of the tower is 40m longer.



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i.e. $BD = h$ metres, $AB = d$ metres and $CA = 40$ metres.

From right angled $\triangle ABD$, we get

$$\tan 60^\circ = \frac{h}{d} \Rightarrow h = \sqrt{3}d \quad \dots \dots \text{(i)}$$

From right angled $\triangle BCD$, we get

$$\tan 30^\circ = \frac{h}{40+d} \Rightarrow \frac{1}{\sqrt{3}} = \frac{\sqrt{3}d}{40+d} \quad [\text{using (i)}]$$

$$\Rightarrow 3d = 40 + d \Rightarrow 2d = 40$$

$$\Rightarrow d = 20$$

$$\text{From (i), } h = 20\sqrt{3} = 20 \times 1.732 = 34.64$$

Hence, the height of the tower is 34.64 m

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Angle of inclination	Angle of elevation	Angle of depression
Formed between the vertical or horizontal as defined by the situation. The angle of inclination with the vertical is 42° .	Formed by looking up from the horizontal The angle of elevation is 36° .	Formed by looking down from the horizontal. The angle of depression is 23° .